

Figure 1 (a, b)

Tessellation with proof of the pythagorean theorem
 [[I.1, 53]]

The line in square brackets indicates the volume and page where the original figure appeared and the section and page where the figure is discussed in the present work. D, Dyck (1880); F, Fricke (1926); F-K, Fricke and Klein (1897, 1912); K-F, Klein and Fricke (1890). Fricke, 1916 refers to: Fricke, R., "Die elliptischen Funktionen und ihre Anwendungen," Vol. 1. B. G. Teubner, Leipzig.

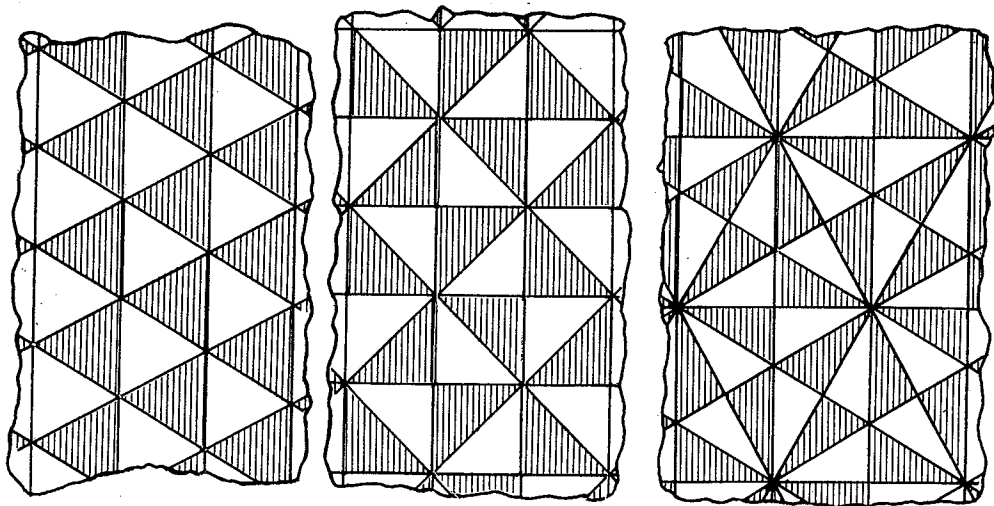


Figure 2 (a, b, c)
 Triangle tessellations of the euclidean plane
 [K-F, 107 II.4, 69, 70]

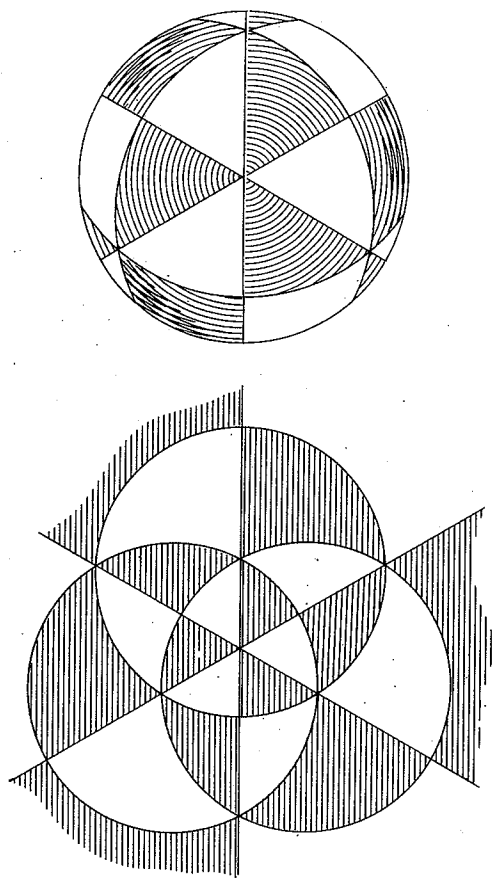


Figure 3 (a, b)
 Tessellation of the tetrahedral group on plane and sphere
 [K-F, 104 II.4, 74]

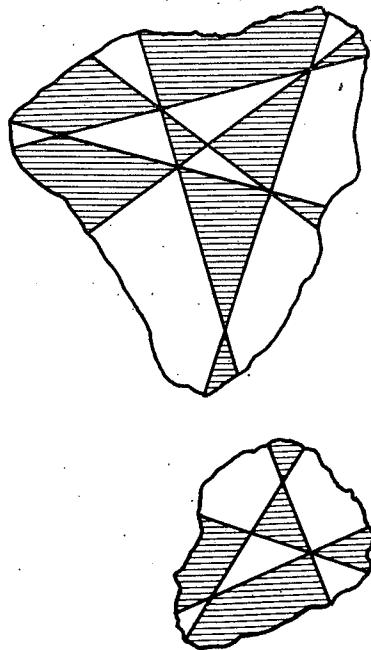


Figure 3 (c)
 Tessellation of the tetrahedral group and a dihedral group in the elliptic plane
 [F-K, 70 II.4, 74]

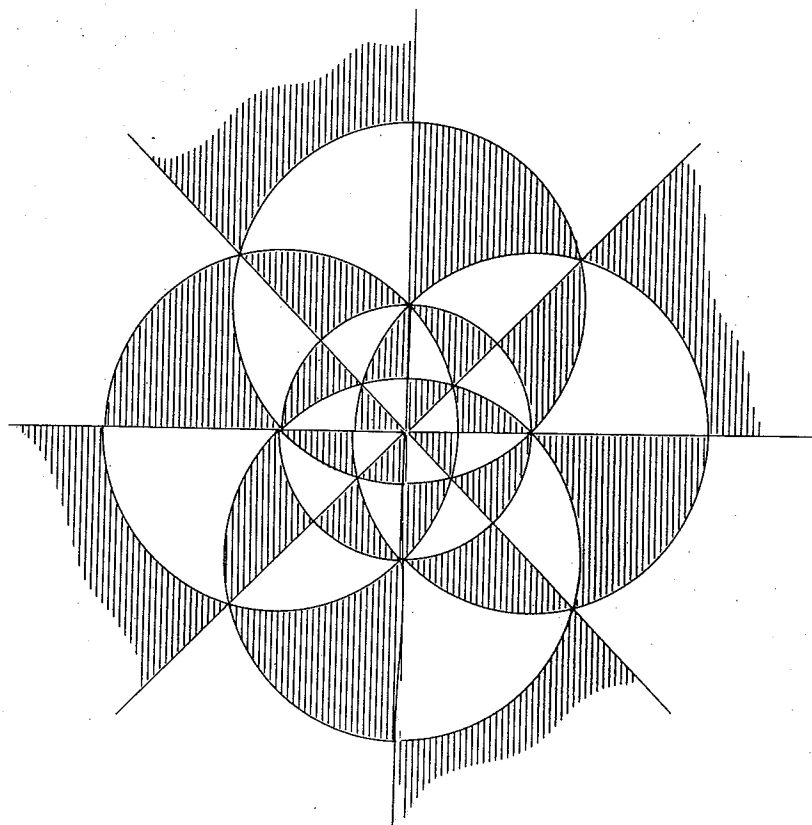


Figure 4 (a)
Tessellation of the octahedral group on plane
[K-F, 75 II.4, 76]

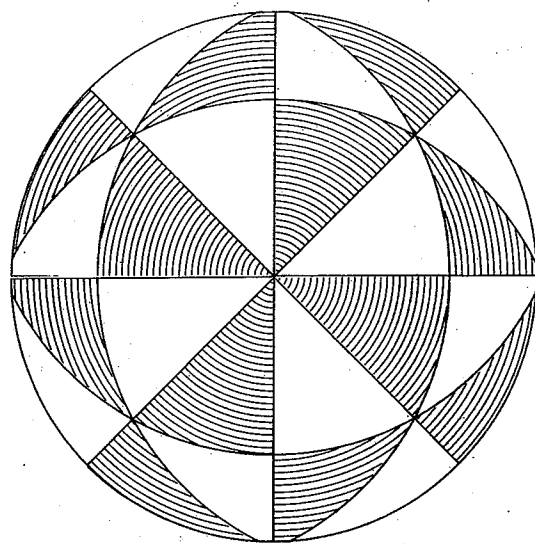


Figure 4 (b)
Tessellation of the octahedral group on sphere
[K-F, 76 II.4, 76]

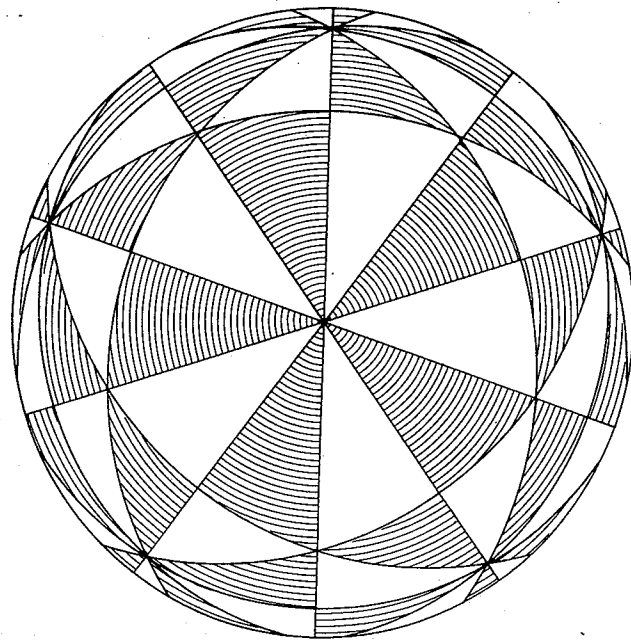


Figure 5 (a)
Tesselation of the group of the icosahedron on sphere
[F, 46 II.4, 76]

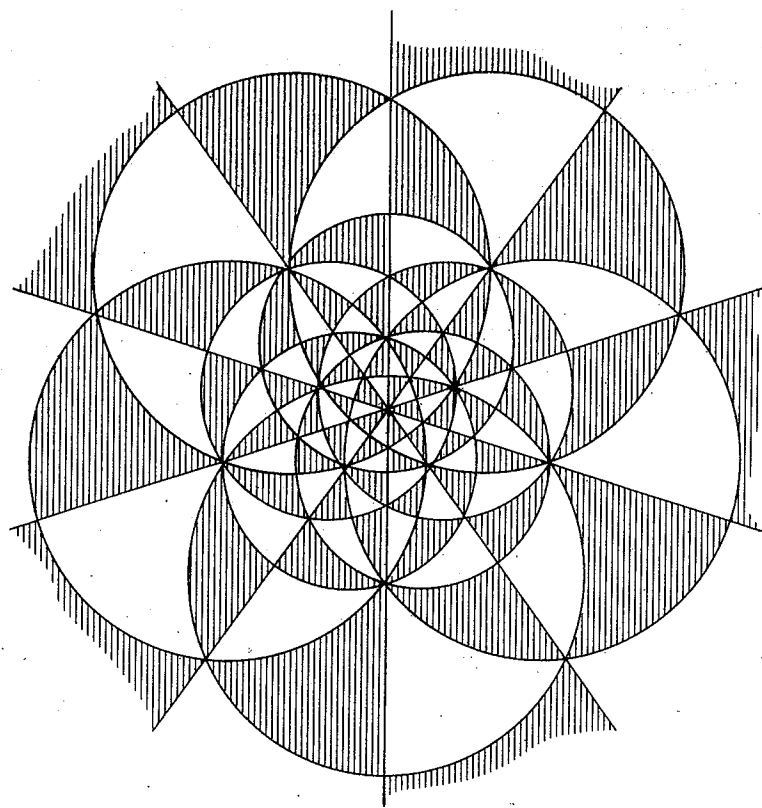


Figure 5 (b)
Tesselation of the group of the icosahedron on plane
[F, 46 II.4, 76]

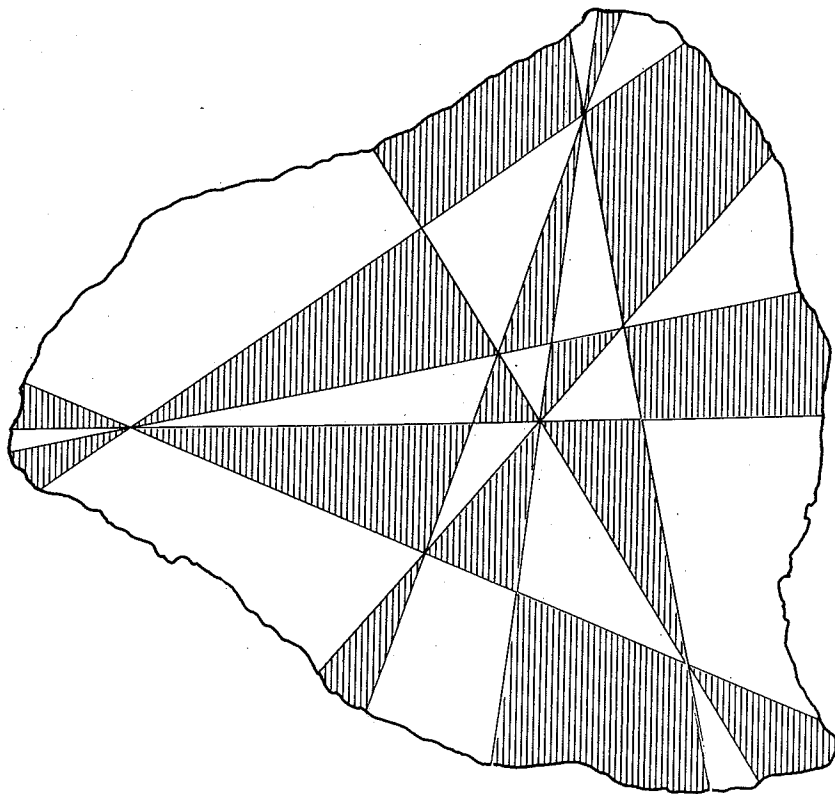


Figure 6
Octahedral tessellation in the elliptic plane
[F-K, 71 II.4, 74]

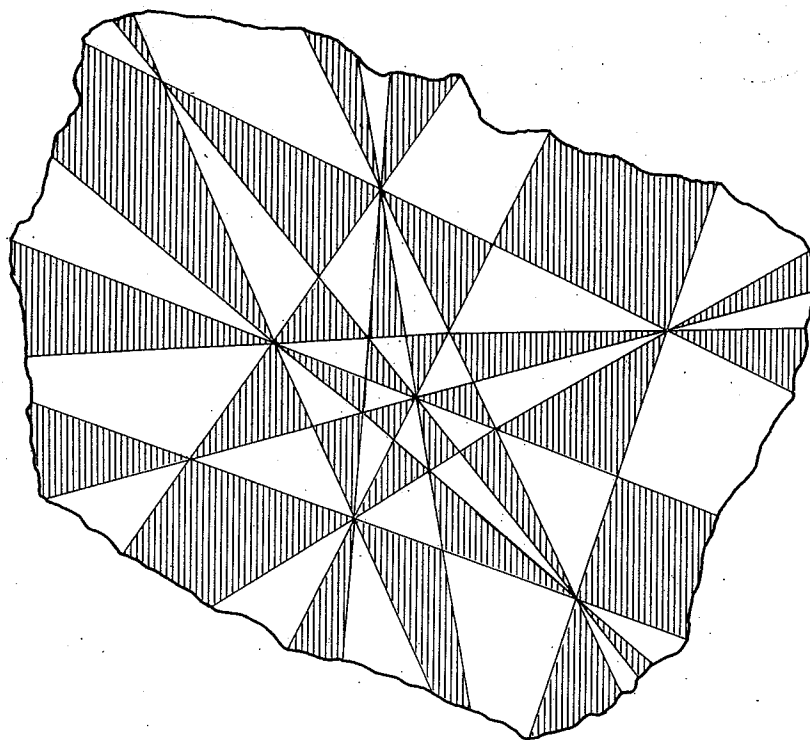


Figure 7
Icosahedral tessellation in the elliptic plane
[F-K, 72 II.4, 76]

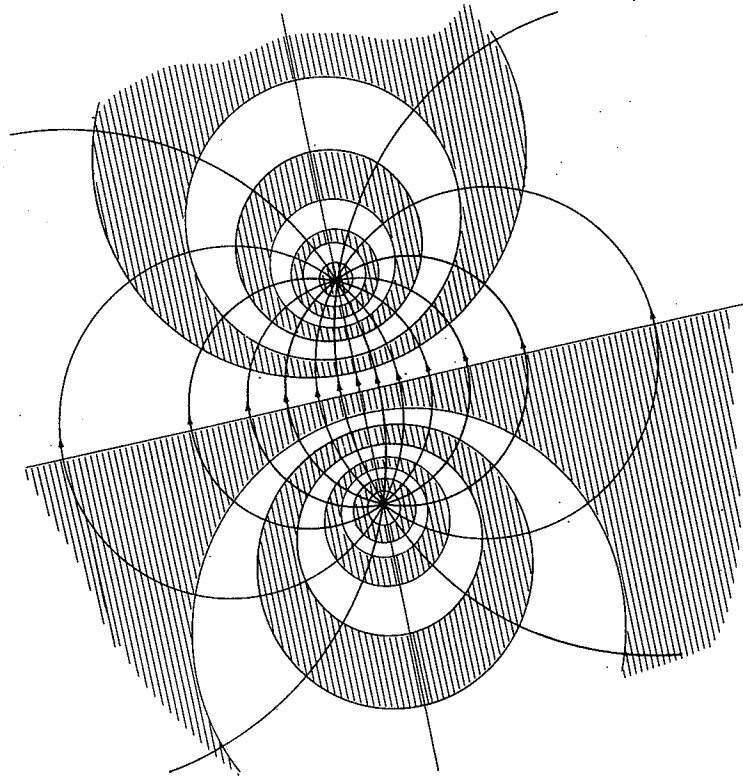


Figure 8 (a)
Orbits of hyperbolic substitution
[K-F, 206 I.2, 10]

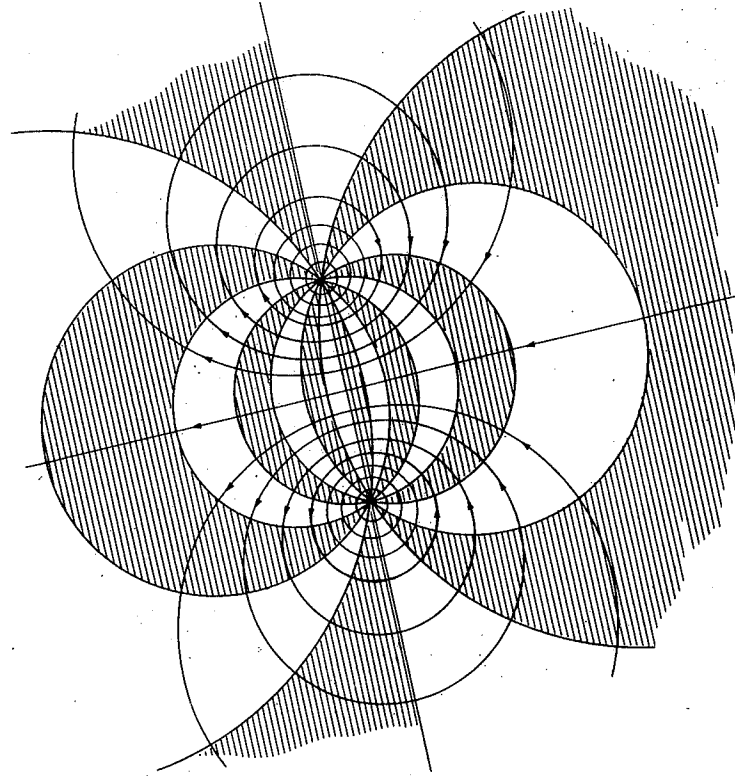


Figure 8 (b)
Orbits of elliptic substitution
[K-F, 206 I.2, 10]

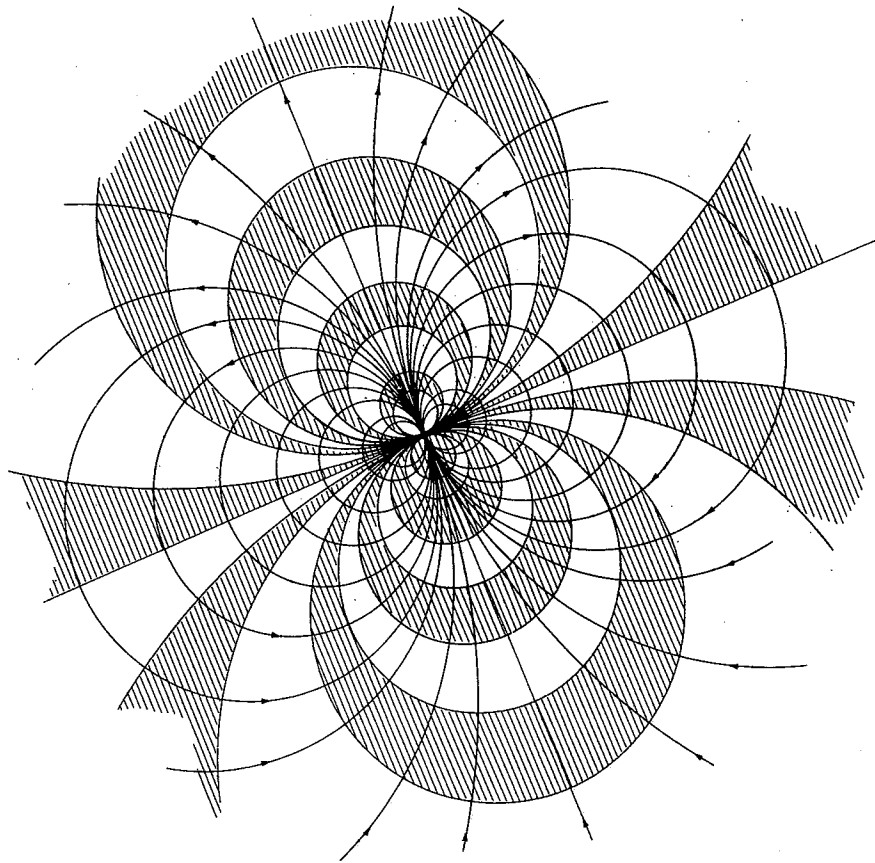


Figure 9
Orbits and their orthogonal trajectories of a parabolic substitution
[K-F, 207 I.2, 10]

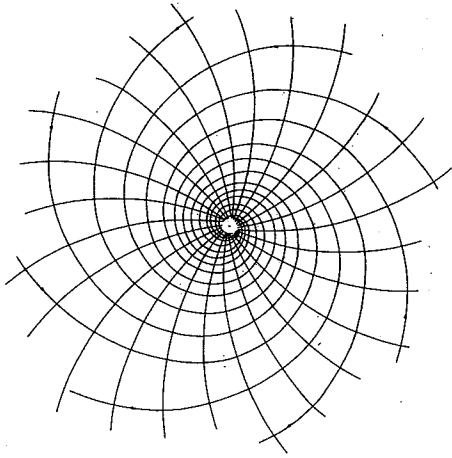


Figure 10
Orbits and their orthogonal trajectories
of loxodromic substitutions with fixed
point at infinity
[K-F, 168 I.2, 10]

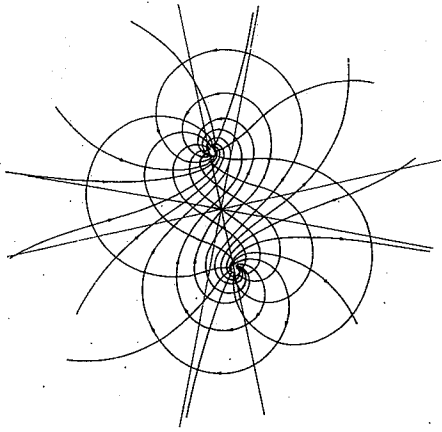


Figure 11
Orbits and their orthogonal trajectories
of loxodromic substitutions with finite
fixed points
[K-F, 172 I.2, 10]

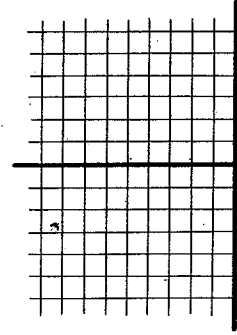


Figure 12
Mapping of halfplane into an ellipse
[F-K, 23 I.6, 42]

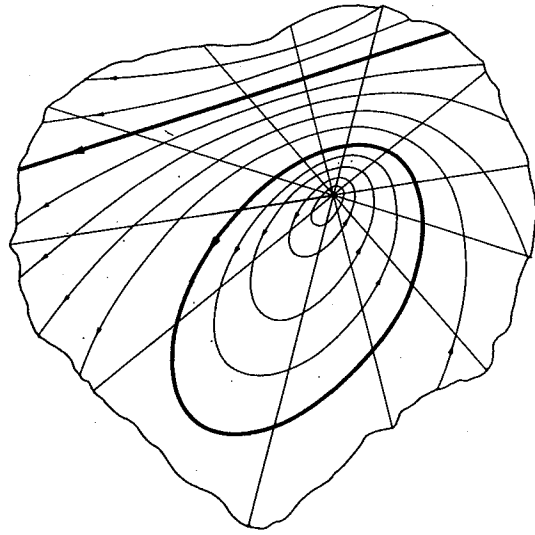
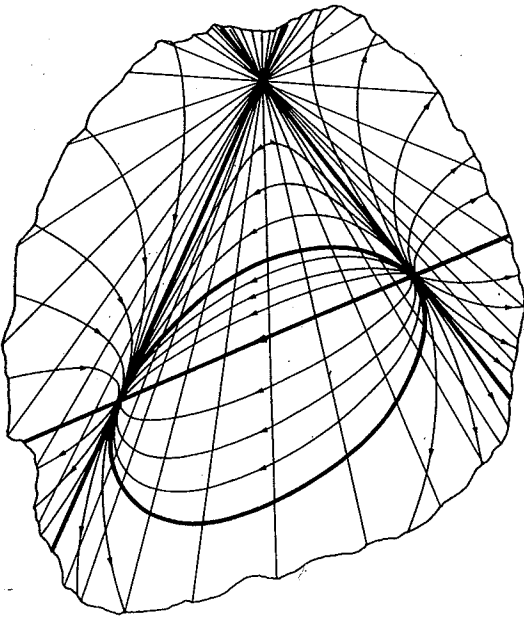


Figure 13 (a, b)
Orbits of hyperbolic and of elliptic substitutions in Klein's projective model
[F-K, 34 I.6, 42]

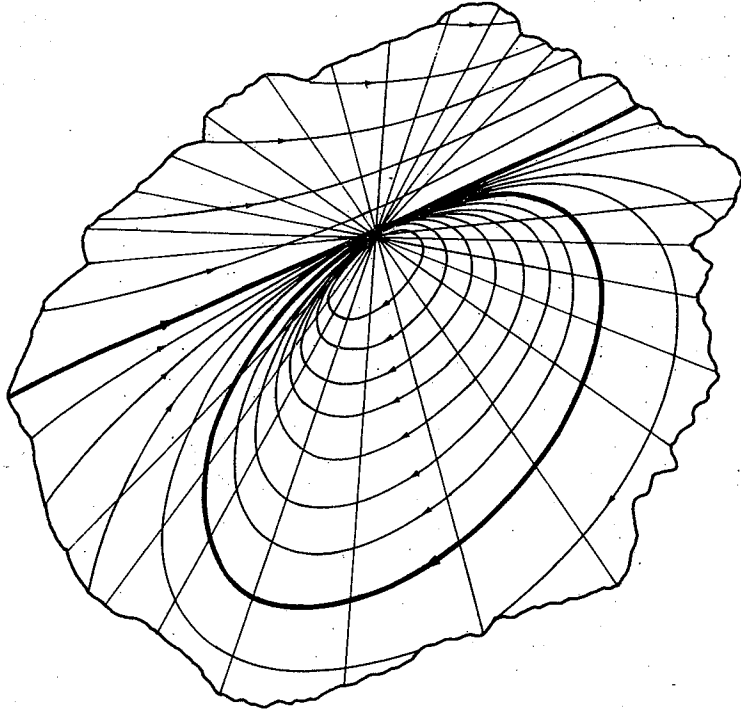


Figure 14
Orbits of parabolic substitutions in Klein's projective model
[F-K, 35 I.6, 42]

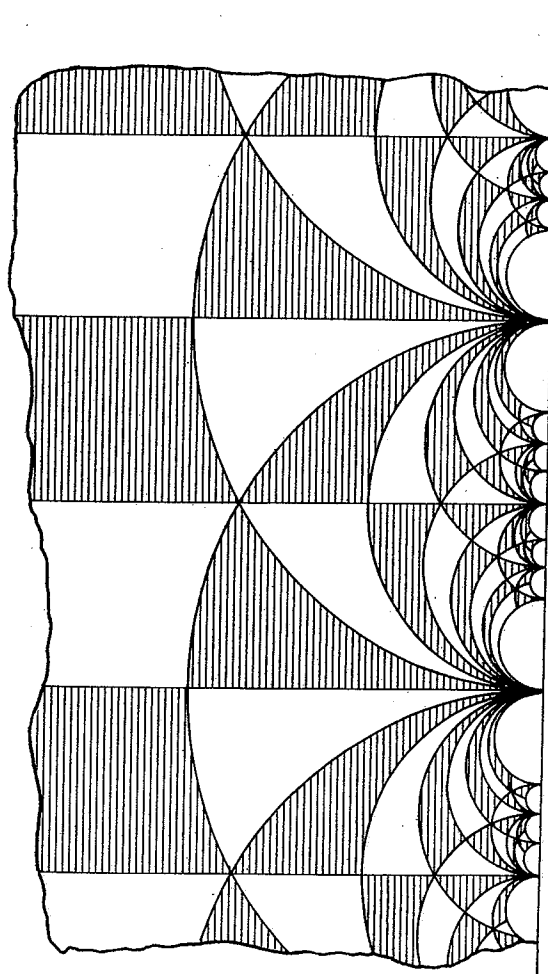


Figure 15

Tesselation of upper halfplane induced by the extended modular group
 [F, 30; II.5, 90; III.1, 111]

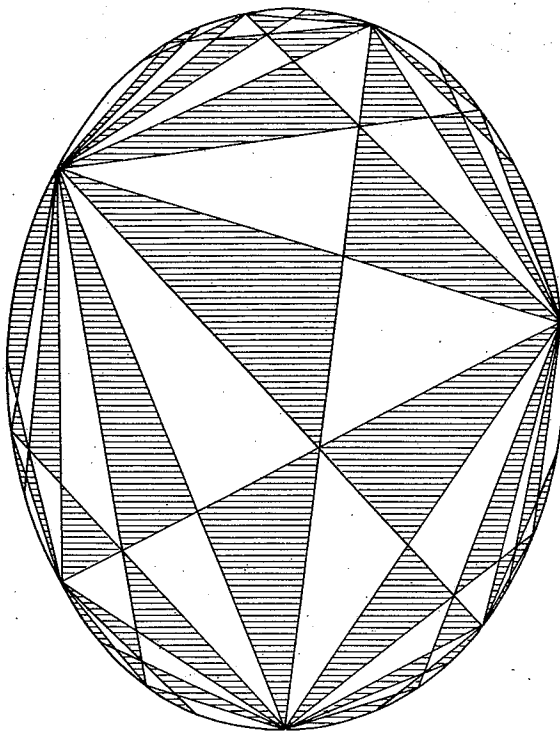


Figure 16

Tesselation of ellipse induced by extended modular group
 [K-F, 289; II.5, 90]

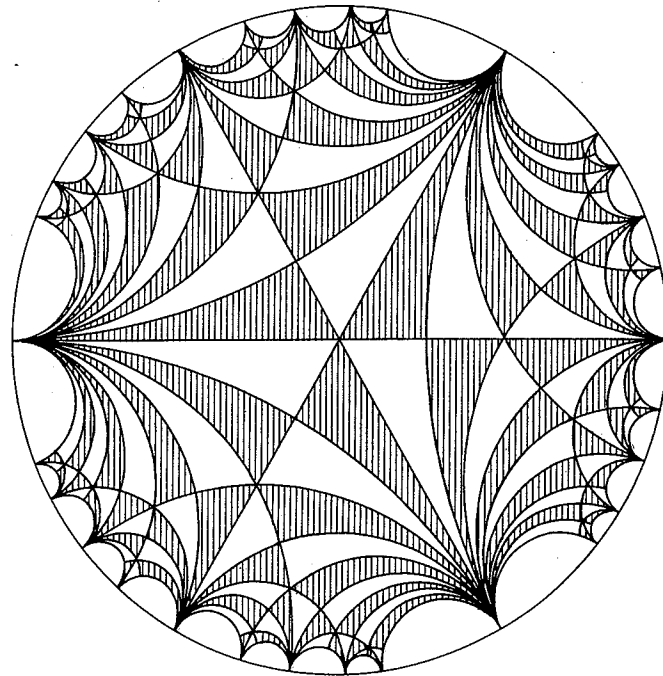


Figure 17
 Tesselation of unit disk induced by extended modular group
 [K-F, 112 III.1, 111, 112; IV.1, 140]

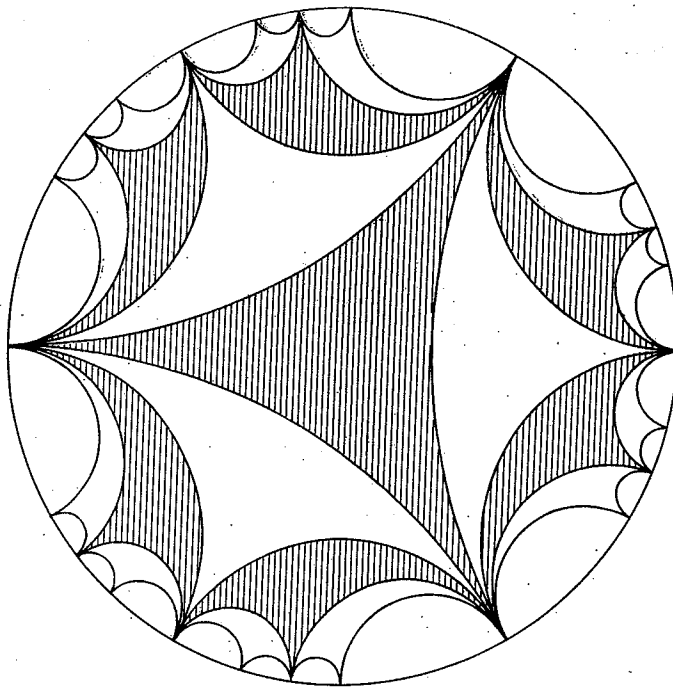


Figure 18
 Tesselation of unit disk induced by repeated reflection of zero-angle triangle
 [K-F, 111 III.2, 112]

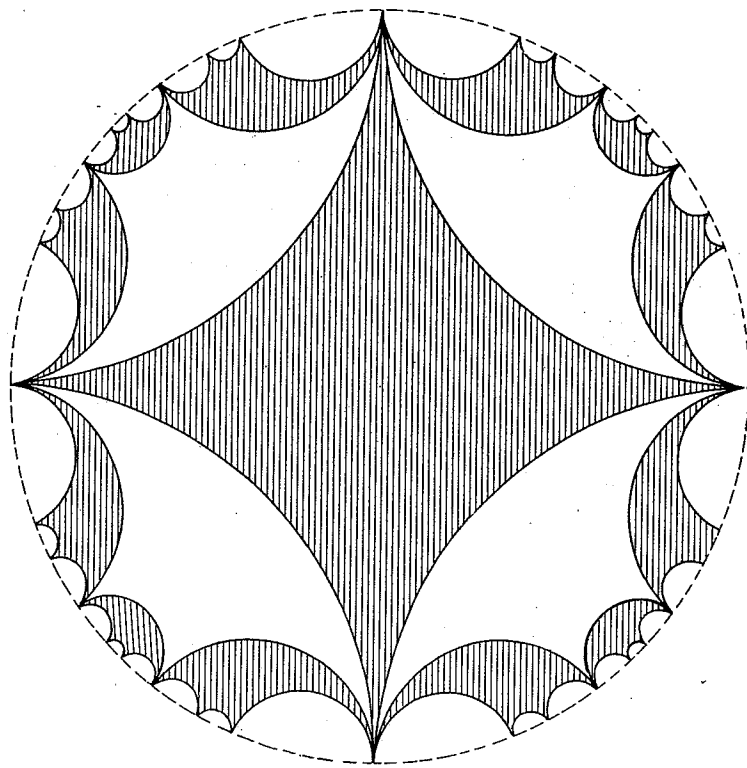


Figure 19 (a)
 Tessellation of the unit disk induced by subgroup of the extended modular group
 [D, 20 III.2, 114; IV.1, 140]

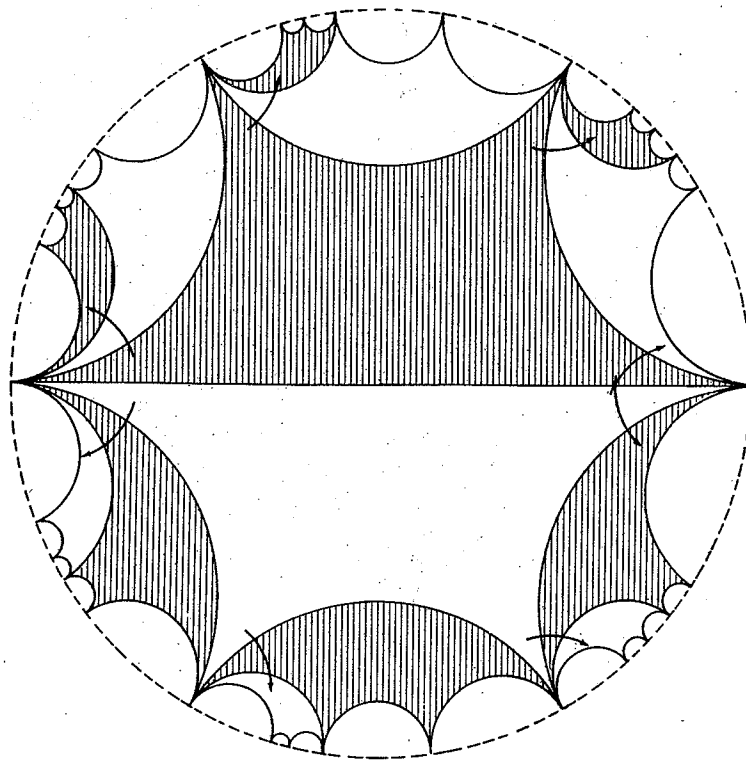


Figure 19 (b)
 Tessellation of the unit disk induced by subgroup of the extended modular group
 [D, 20 III.2, 114; IV.1, 140]

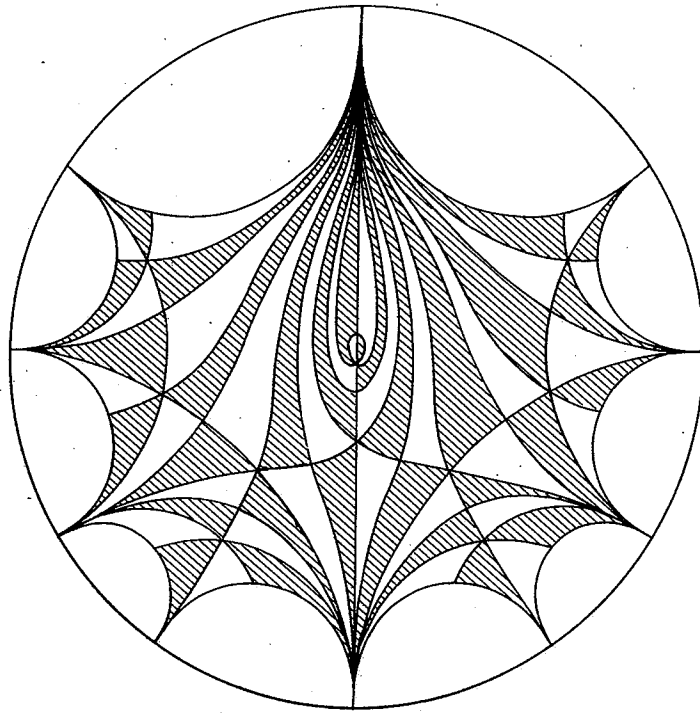


Figure 20
 Image of part of the tessellation induced in the upper halfplane by the extended modular group under an exponential mapping
 [Fricke (1916, 300) II.5, 90]

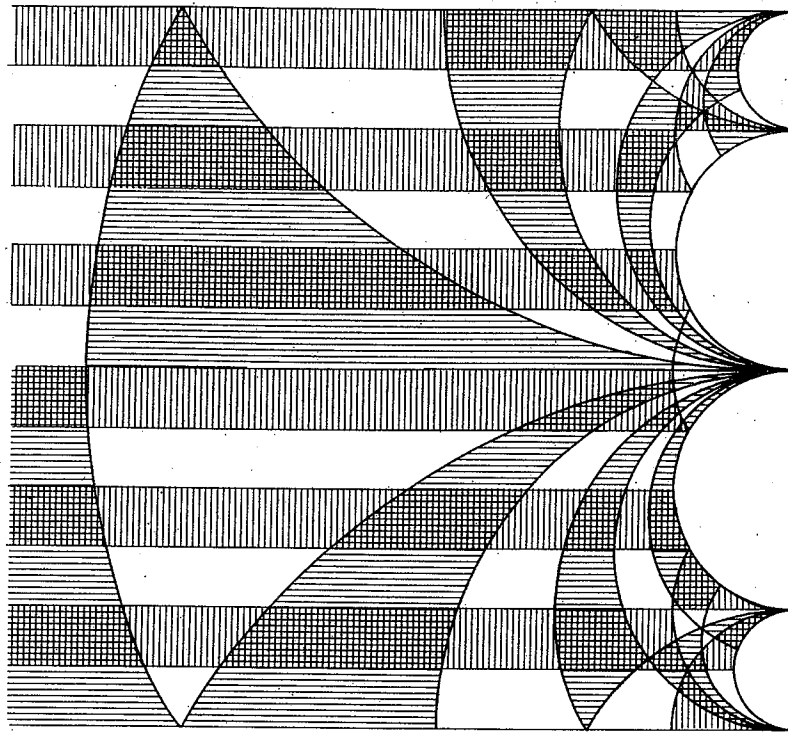


Figure 21
 Superposition of two tessellations induced by the modular group
 [F-K, 549 III.3, 126]

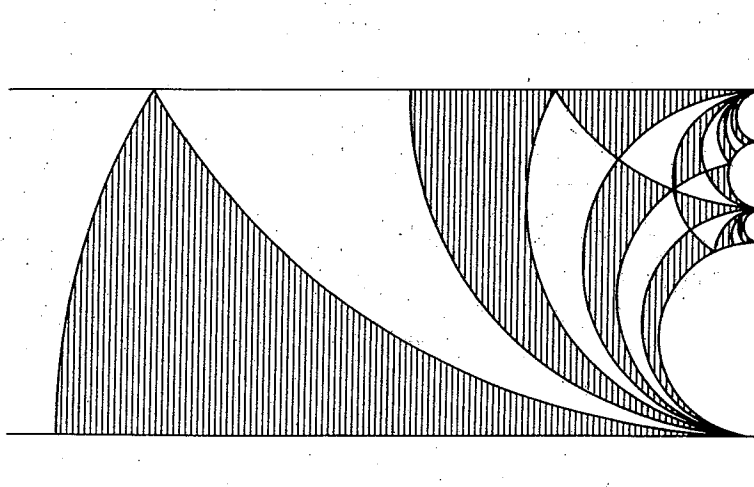


Figure 22
Part of tessellation induced by the extended modular group
[K-F, 373 III.2, 115]

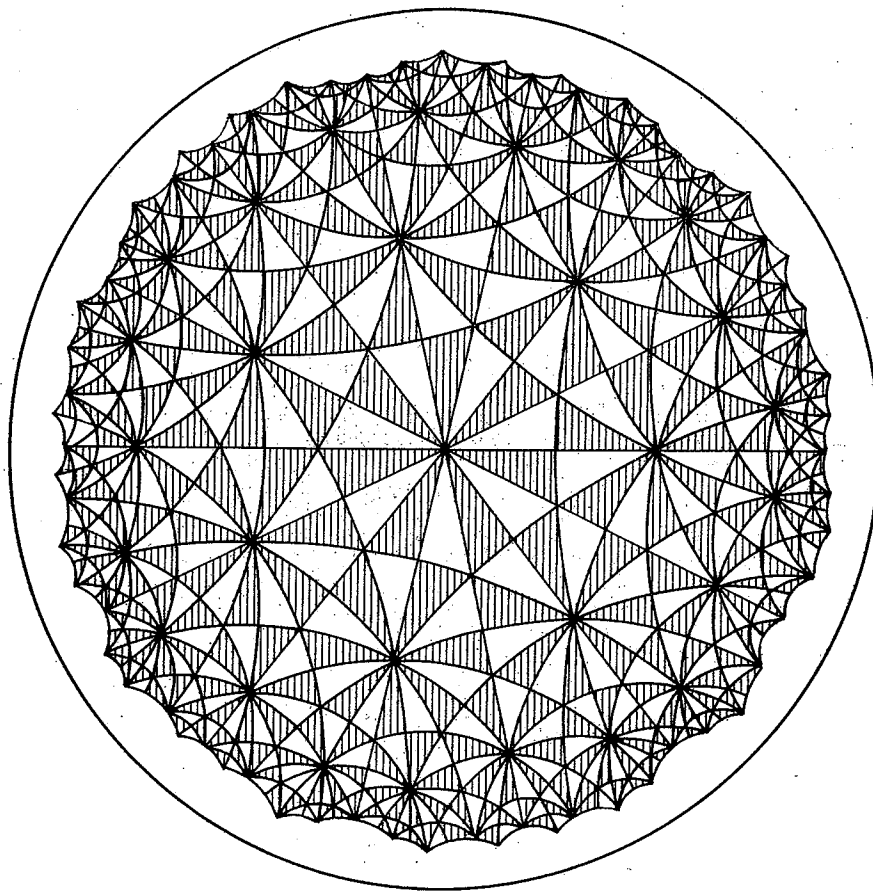


Figure 23
Tessellation of the unit disk belonging to the triangle group $T^*(2, 3, 7)$
[K-F, 109 II.5, 90]

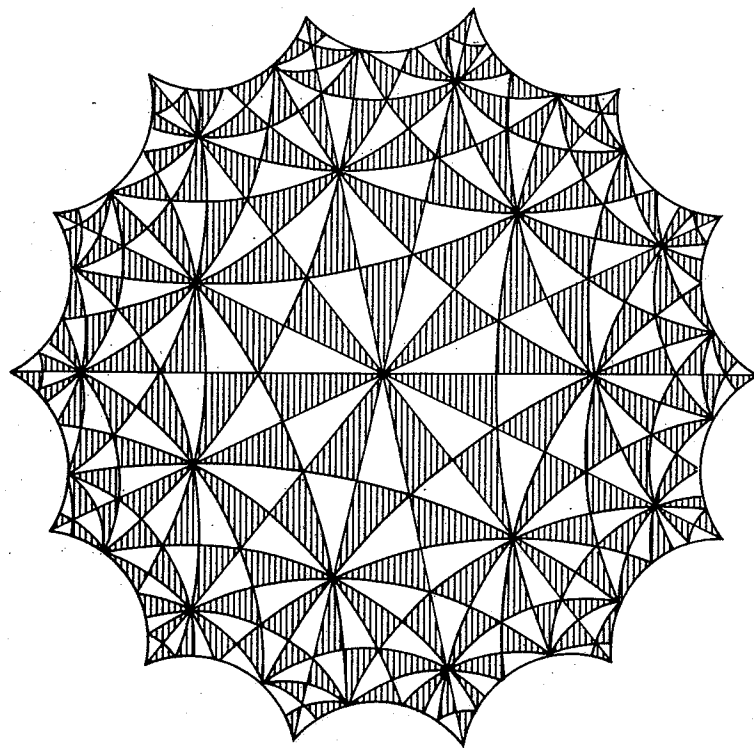


Figure 24

Fundamental region of a subgroup of index 168 in $T(2, 3, 7)$
[K-F, 370 II.6, 94]

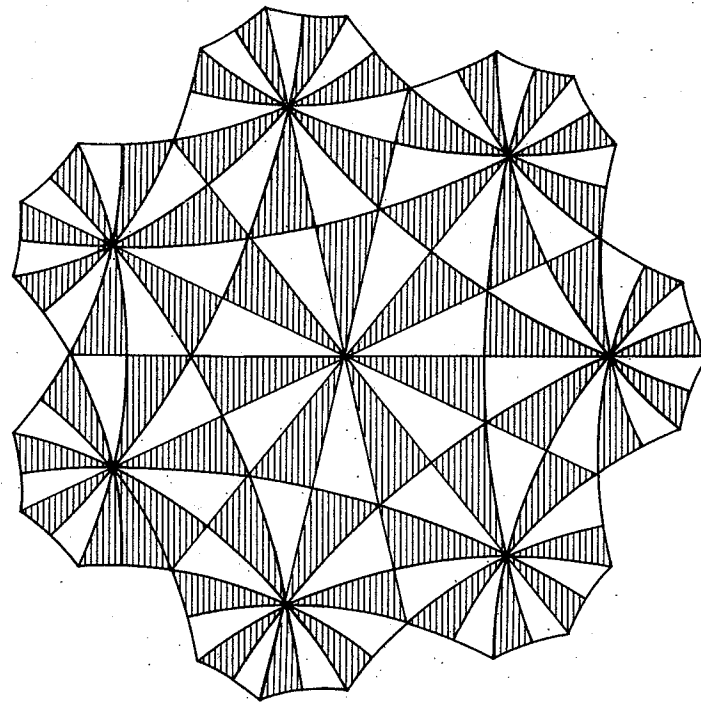


Figure 25

A heptagon and its seven neighbors in the tessellation of $T(2, 3, 7)$
[K-F, 464 II.6, 95]

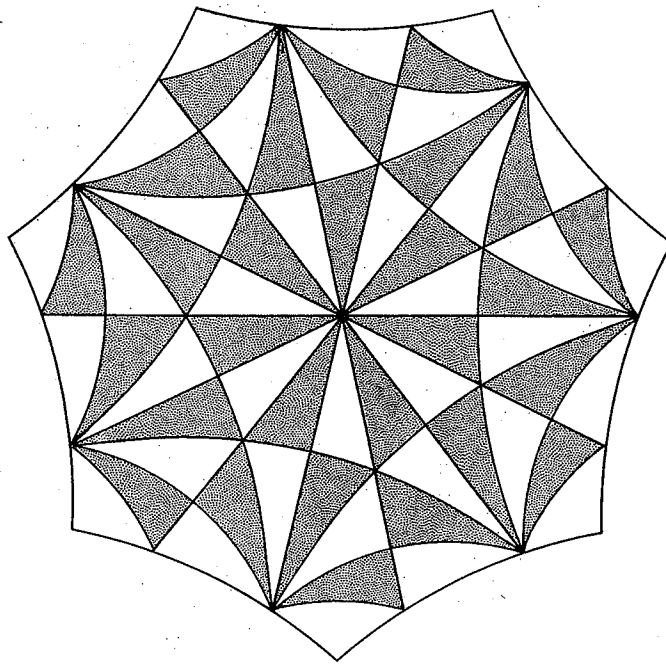


Figure 26
 Unsymmetric tessellation of a regular heptagon by 63 triangles with
 angles $\pi/2, \pi/3, \pi/7$
 [F-K, 621 II.6, 95]

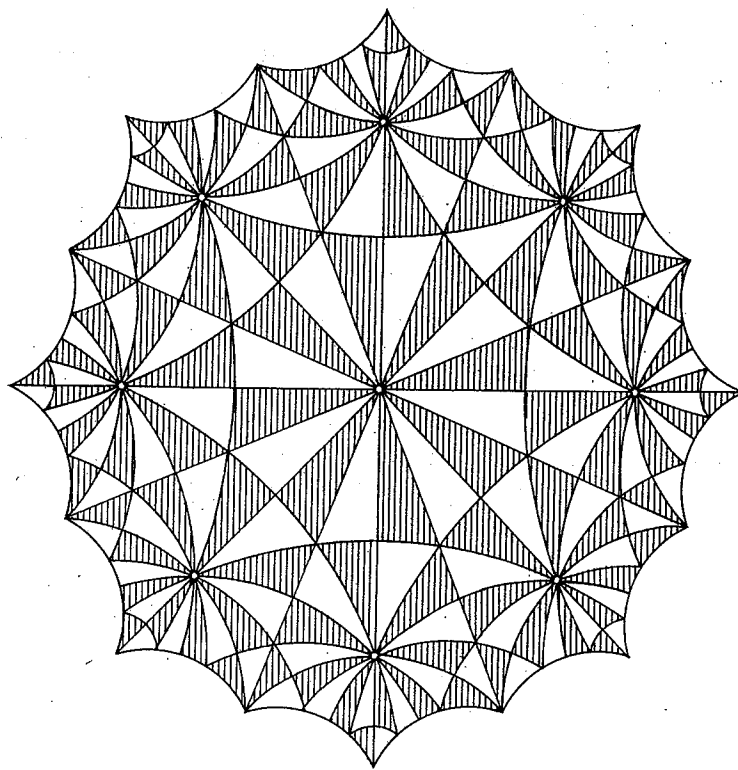


Figure 27
 Tessellation by the triangle group $T^*(2, 3, 8)$
 [D, 17 II.6, 94]

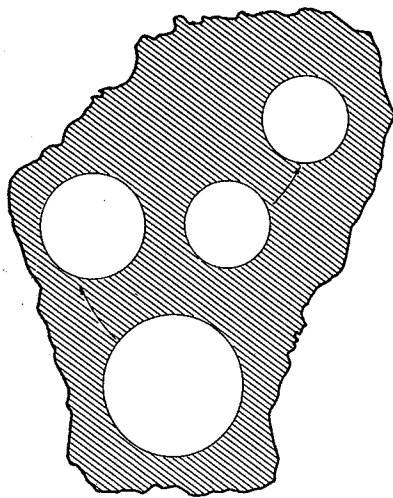


Figure 28
Composition of two cyclic groups of infinite order.
[F-K, 191 IV.1, 135]

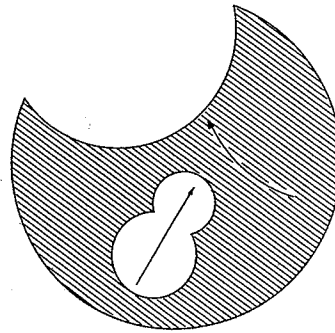


Figure 29
Composition of two cyclic groups of finite order.
[F-K, 191 IV.1, 135]

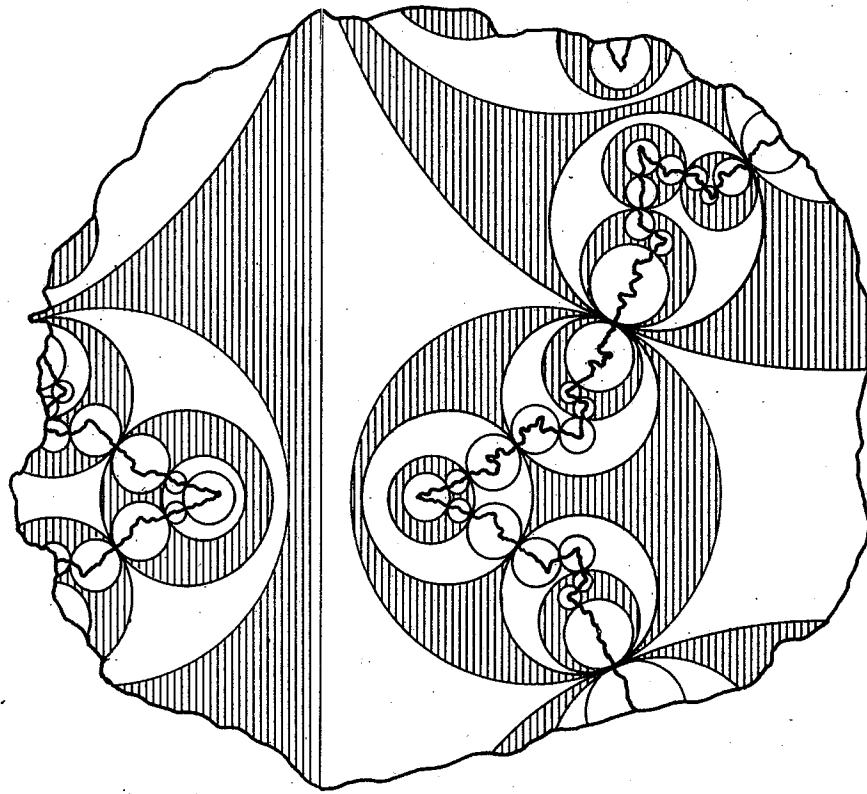


Figure 30
Tessellation and nondifferentiable curve of limit points for nonfuchsian group.
[F-K, 418 IV.1, 146]

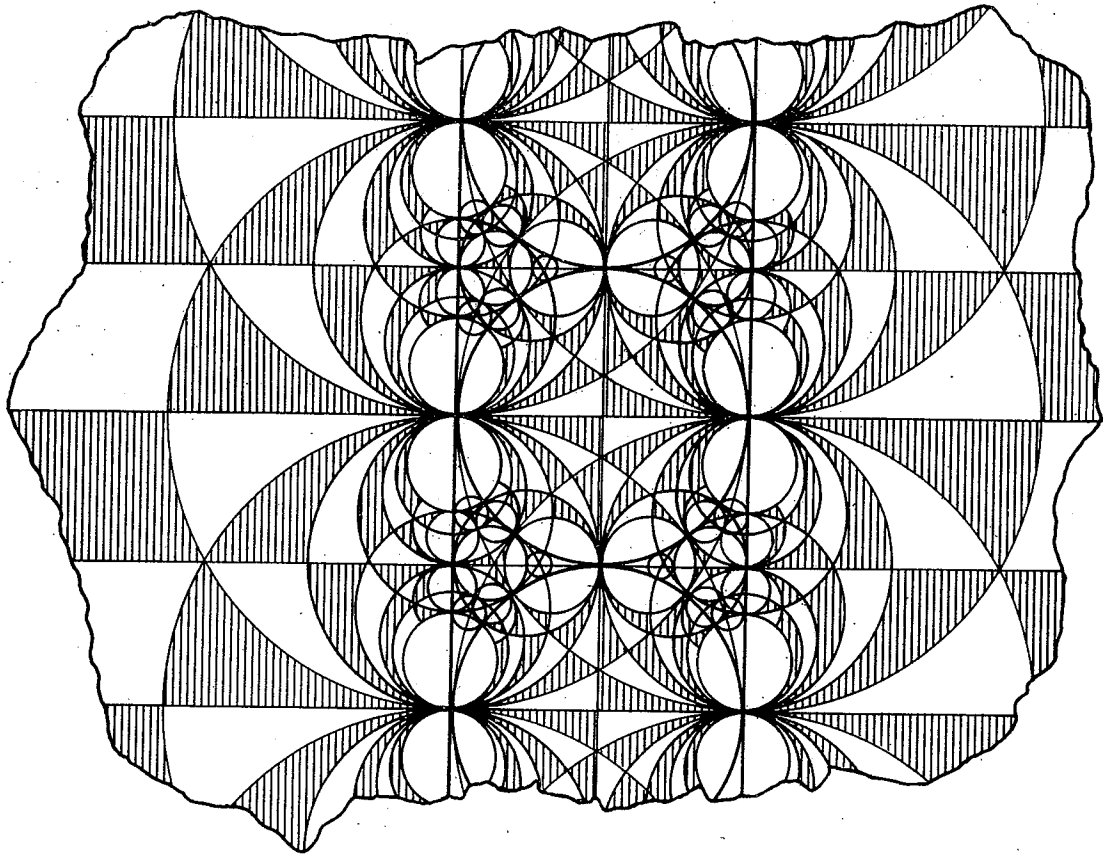


Figure 32
 Degenerate form of tessellation in Figure 30
 [F-K, 482 IV.1, 147]

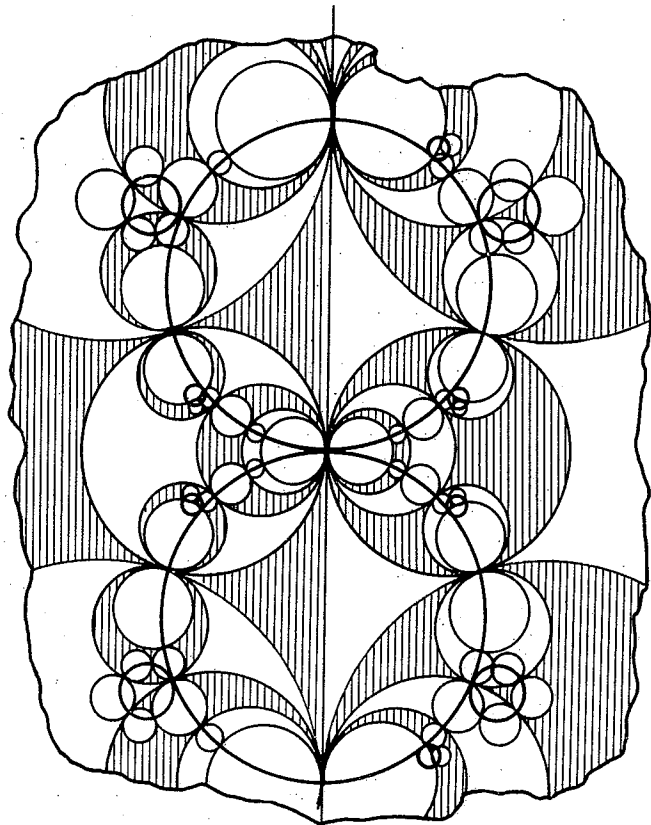


Figure 31
 Tessellation of nonfuchsian group with infinitely many limit circles
 [F-K, 429 IV.1, 147]

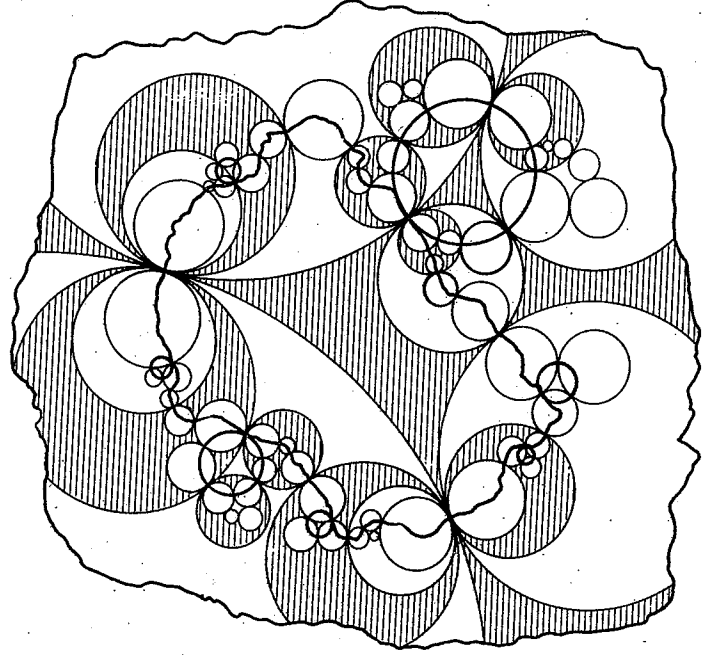


Figure 34
 Tessellation with nondifferentiable curve of limit points and with limit circles
 [F-K, 440 IV.1, 147]

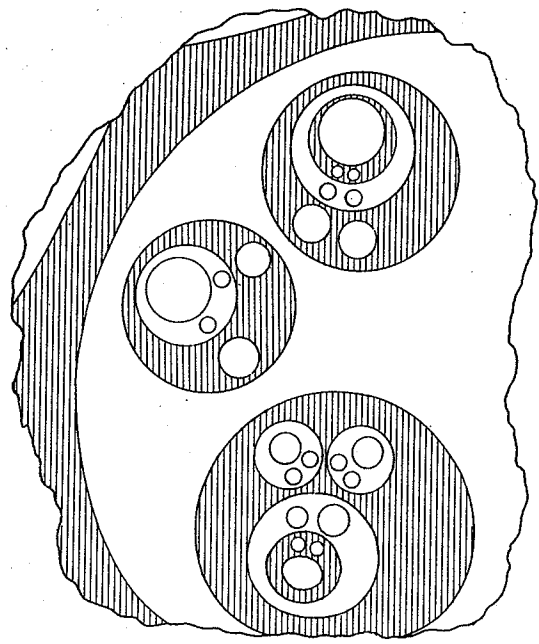


Figure 33
 Tessellation arising from reflections in four disjoint circles
 [F-K, 437 IV.1, 147]

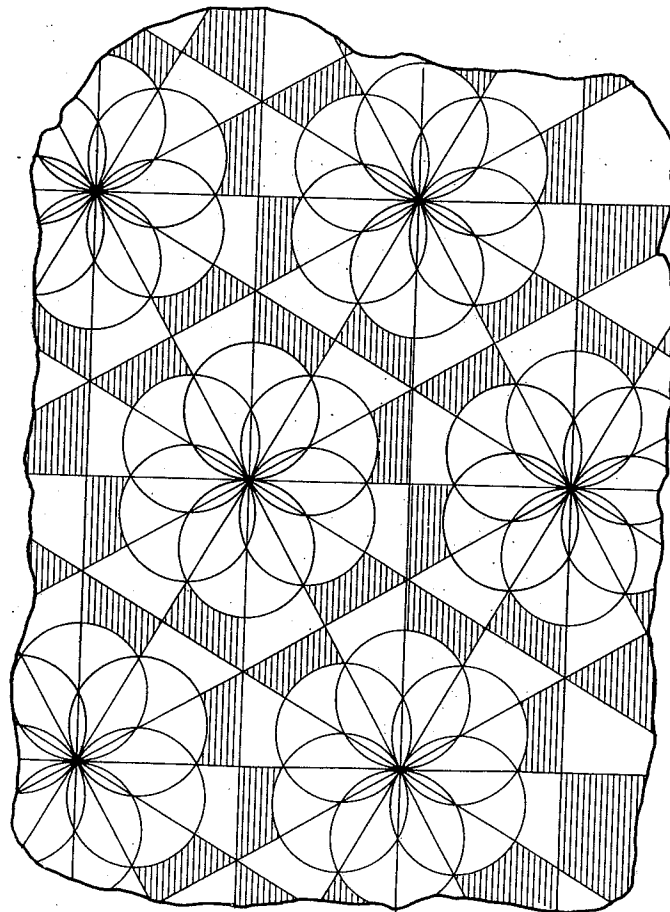


Figure 35

Tessellation arising from composition of two euclidean triangle groups
[F-K, 433 IV.1, 147]

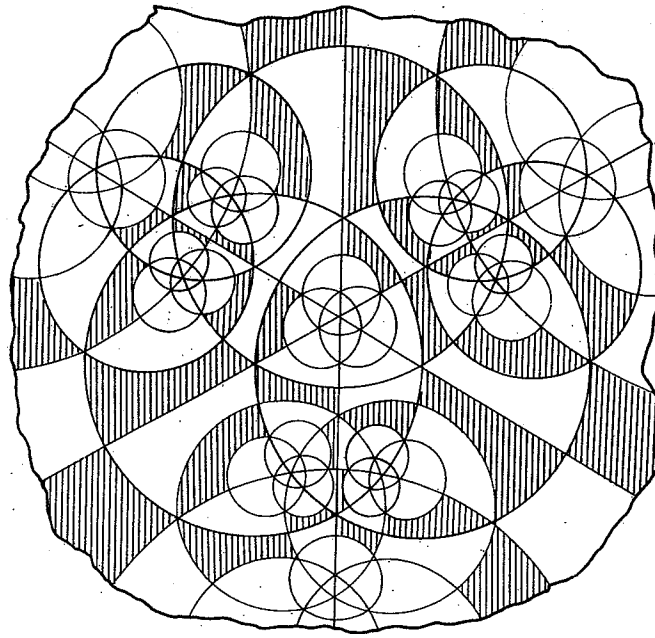


Figure 36

Tessellation arising from composition of two tetrahedral groups
[F-K, 435 IV.1, 147]

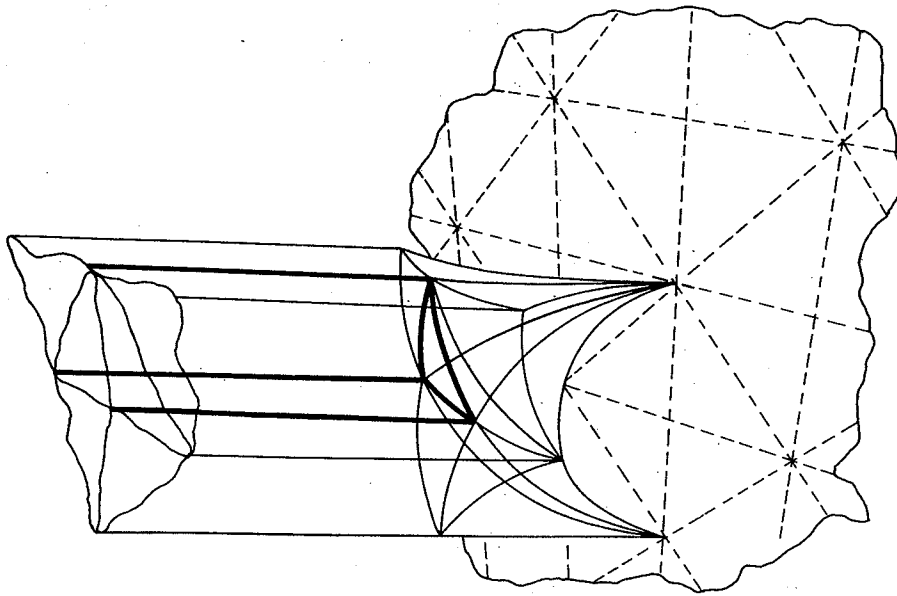


Figure 37
 Fundamental region of Picard's group
 [F-K, 82 V.1, 152]

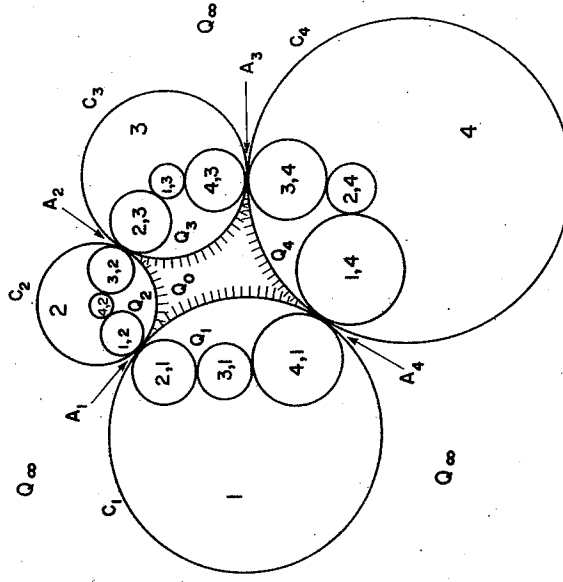


Figure 38
 First step in the construction of the tessellation induced by a special nonfuchsian group
 [IV.1, 137]

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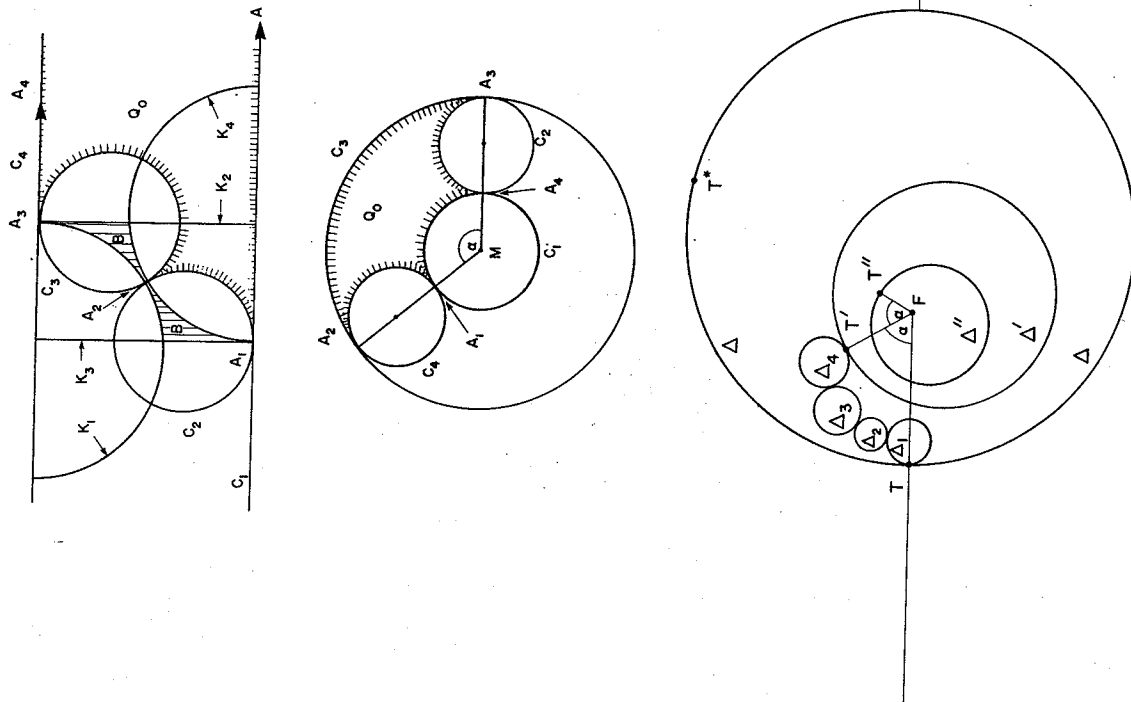


Figure 39

Behavior of nondifferentiable limit point curve near: (a) parabolic fixed point [IV.1, 143]; (b) hyperbolic fixed point [IV.1, 145]; (c) loxodromic fixed point [IV.1, 146].